**Homework 4 -Sadiya Amreen**

Problem 3 (25 points):

In this problem we will continue with the wine quality data from Problem 1, but this time we will use clustering. Do not forget to remove the type variable before clustering because that would be cheating by using the label to perform clustering. a. Use k-means to cluster the data. Show your usage of silhouette and the elbow method to pick the best number of clusters. Make sure it is using multiple restarts.

library(factoextra)

## Warning: package 'factoextra' was built under R version 4.2.2

## Loading required package: ggplot2

## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

library(ggplot2)  
library(lattice)  
library(dplyr)

##   
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':  
##   
## filter, lag

## The following objects are masked from 'package:base':  
##   
## intersect, setdiff, setequal, union

library(caret)  
library(tidyverse)

## ── Attaching packages  
## ───────────────────────────────────────  
## tidyverse 1.3.2 ──

## ✔ tibble 3.1.8 ✔ purrr 0.3.4  
## ✔ tidyr 1.2.1 ✔ stringr 1.4.1  
## ✔ readr 2.1.2 ✔ forcats 0.5.2  
## ── Conflicts ────────────────────────────────────────── tidyverse\_conflicts() ──  
## ✖ dplyr::filter() masks stats::filter()  
## ✖ dplyr::lag() masks stats::lag()  
## ✖ purrr::lift() masks caret::lift()

library(stats)

wwine <- read.csv("C:/Sadiya Studies/Data Science/DS441-Fundamts DS/homework/1-winequality-WHITE.csv", header = TRUE,sep = ";")  
rwine <- read.csv("C:/Sadiya Studies/Data Science/DS441-Fundamts DS/homework/2-winequality-RED.csv", header = TRUE,sep = ";")  
#Combining the White wine and Red wine using the full join. As I'm starting it as a new one so that  
#I don't want to remove the type coloumn from the wine data.  
w\_plot\_d <- full\_join(wwine,rwine)

## Joining, by = c("fixed.acidity", "volatile.acidity", "citric.acid",  
## "residual.sugar", "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide",  
## "density", "pH", "sulphates", "alcohol", "quality")

w\_plot\_d <- na.omit(w\_plot\_d)  
#for 3c  
rwine3 <- rwine  
wwine3 <- wwine  
wwine3$type <- "white"  
rwine3$type <- "red"  
wine\_data <- full\_join(wwine3,rwine3)

## Joining, by = c("fixed.acidity", "volatile.acidity", "citric.acid",  
## "residual.sugar", "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide",  
## "density", "pH", "sulphates", "alcohol", "quality", "type")

wine\_data <- na.omit(wine\_data)  
str(wine\_data)

## 'data.frame': 6497 obs. of 13 variables:  
## $ fixed.acidity : num 7 6.3 8.1 7.2 7.2 8.1 6.2 7 6.3 8.1 ...  
## $ volatile.acidity : num 0.27 0.3 0.28 0.23 0.23 0.28 0.32 0.27 0.3 0.22 ...  
## $ citric.acid : num 0.36 0.34 0.4 0.32 0.32 0.4 0.16 0.36 0.34 0.43 ...  
## $ residual.sugar : num 20.7 1.6 6.9 8.5 8.5 6.9 7 20.7 1.6 1.5 ...  
## $ chlorides : num 0.045 0.049 0.05 0.058 0.058 0.05 0.045 0.045 0.049 0.044 ...  
## $ free.sulfur.dioxide : num 45 14 30 47 47 30 30 45 14 28 ...  
## $ total.sulfur.dioxide: num 170 132 97 186 186 97 136 170 132 129 ...  
## $ density : num 1.001 0.994 0.995 0.996 0.996 ...  
## $ pH : num 3 3.3 3.26 3.19 3.19 3.26 3.18 3 3.3 3.22 ...  
## $ sulphates : num 0.45 0.49 0.44 0.4 0.4 0.44 0.47 0.45 0.49 0.45 ...  
## $ alcohol : num 8.8 9.5 10.1 9.9 9.9 10.1 9.6 8.8 9.5 11 ...  
## $ quality : int 6 6 6 6 6 6 6 6 6 6 ...  
## $ type : chr "white" "white" "white" "white" ...

wine\_data\_re <- wine\_data[-c(56,78),]  
str(wine\_data\_re)

## 'data.frame': 6495 obs. of 13 variables:  
## $ fixed.acidity : num 7 6.3 8.1 7.2 7.2 8.1 6.2 7 6.3 8.1 ...  
## $ volatile.acidity : num 0.27 0.3 0.28 0.23 0.23 0.28 0.32 0.27 0.3 0.22 ...  
## $ citric.acid : num 0.36 0.34 0.4 0.32 0.32 0.4 0.16 0.36 0.34 0.43 ...  
## $ residual.sugar : num 20.7 1.6 6.9 8.5 8.5 6.9 7 20.7 1.6 1.5 ...  
## $ chlorides : num 0.045 0.049 0.05 0.058 0.058 0.05 0.045 0.045 0.049 0.044 ...  
## $ free.sulfur.dioxide : num 45 14 30 47 47 30 30 45 14 28 ...  
## $ total.sulfur.dioxide: num 170 132 97 186 186 97 136 170 132 129 ...  
## $ density : num 1.001 0.994 0.995 0.996 0.996 ...  
## $ pH : num 3 3.3 3.26 3.19 3.19 3.26 3.18 3 3.3 3.22 ...  
## $ sulphates : num 0.45 0.49 0.44 0.4 0.4 0.44 0.47 0.45 0.49 0.45 ...  
## $ alcohol : num 8.8 9.5 10.1 9.9 9.9 10.1 9.6 8.8 9.5 11 ...  
## $ quality : int 6 6 6 6 6 6 6 6 6 6 ...  
## $ type : chr "white" "white" "white" "white" ...

##DATA READY TO USE

library(cluster)  
library(kknn)

## Warning: package 'kknn' was built under R version 4.2.2

##   
## Attaching package: 'kknn'

## The following object is masked from 'package:caret':  
##   
## contr.dummy

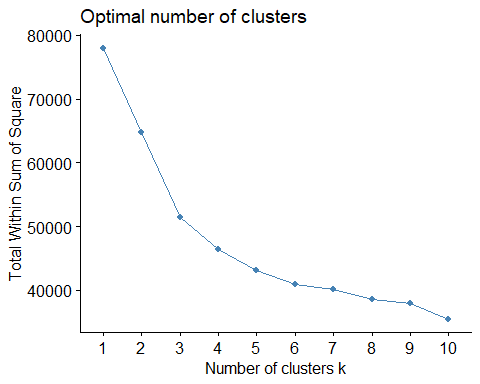
library(mlbench)

## Warning: package 'mlbench' was built under R version 4.2.2

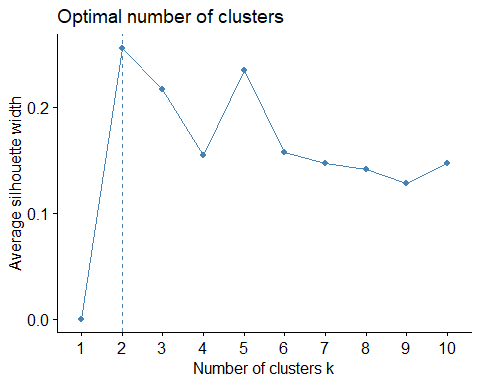
library(stats)  
library(ggfortify)

## Warning: package 'ggfortify' was built under R version 4.2.2

set.seed(123)  
preproc <- preProcess(w\_plot\_d , method=c("center", "scale"))  
predictors <- predict(preproc, w\_plot\_d)  
###\_\_\_K-Means\_\_\_###  
fviz\_nbclust(predictors, kmeans, method = "wss")#method-Elbow



fviz\_nbclust(predictors, kmeans, method = "silhouette")#method-ESilhouette

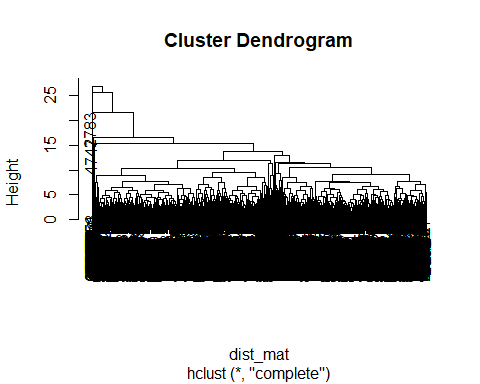
 The K centre is 3 = K by analyzing the silhoute and Elbow method its concluded with K = 3 becuase Silhoute suggests K = 2 but the elbow has the mean value at 3, So the Centre value which is selected is K = 3.

set.seed(240)  
w\_fit\_d <- kmeans(predictors, centers = 3, nstart = 25)#fit the data  
head(w\_fit\_d)

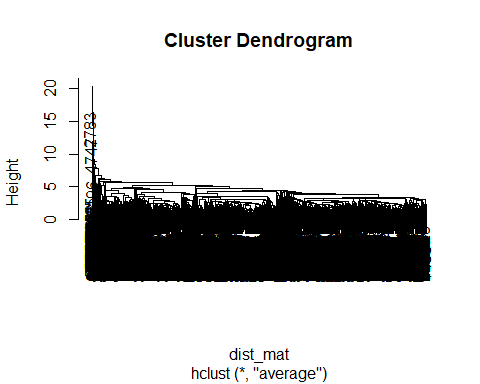
## $cluster  
## 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16   
## 2 3 3 2 2 3 2 2 3 3 3 3 3 3 2 3   
## 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32   
## 3 3 3 2 3 3 3 1 3 2 3 2 3 3 2 3   
## 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48   
## 3 3 2 3 3 3 2 2 2 2 2 3 3 3 2 2   
## 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64   
## 2 2 3 3 3 3 2 3 2 2 3 3 2 2 3 3   
## 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80   
## 3 3 3 2 3 2 2 2 2 3 3 2 3 3 2 2   
## 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96   
## 3 2 2 2 2 2 2 2 2 2 2 2 3 3 3 2   
## 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112   
## 2 3 2 2 2 2 2 2 2 2 2 2 2 3 2 2   
## 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128   
## 2 2 2 1 3 3 2 2 3 2 2 3 3 3 3 2   
## 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144   
## 3 3 3 2 2 2 2 2 3 2 3 3 3 2 3 3   
## 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160   
## 3 3 3 1 3 3 3 2 3 3 1 2 2 3 3 3   
## 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176   
## 3 2 3 2 2 2 2 3 2 2 3 3 3 3 2 3   
## 177 178 179 180 181 182 183 184 185 186 187 188 189 190 191 192   
## 3 2 1 2 2 2 2 2 2 2 2 3 3 2 2 2   
## 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207 208   
## 3 3 2 2 2 2 2 2 2 2 2 3 3 2 2 2   
## 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224   
## 1 3 3 3 2 3 3 2 2 2 2 2 2 2 3 3   
## 225 226 227 228 229 230 231 232 233 234 235 236 237 238 239 240   
## 3 2 3 2 3 2 2 2 2 2 2 2 2 2 3 2   
## 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255 256   
## 2 3 3 2 2 3 3 3 3 2 2 2 2 3 3 3   
## 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272   
## 3 3 3 3 3 2 3 2 3 2 2 2 3 3 2 2   
## 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288   
## 2 2 2 2 2 3 3 3 3 3 2 2 2 2 2 2   
## 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304   
## 2 2 2 3 2 3 2 3 2 3 2 3 3 3 3 3   
## 305 306 307 308 309 310 311 312 313 314 315 316 317 318 319 320   
## 2 2 2 2 3 3 3 3 3 2 2 2 3 3 3 3   
## 321 322 323 324 325 326 327 328 329 330 331 332 333 334 335 336   
## 3 3 3 2 3 2 2 3 2 3 3 3 3 2 3 3   
## 337 338 339 340 341 342 343 344 345 346 347 348 349 350 351 352   
## 3 2 3 3 2 3 2 3 3 3 3 2 2 2 3 3   
## 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367 368   
## 3 3 2 2 2 3 3 3 2 3 3 2 3 3 3 3   
## 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383 384   
## 3 3 3 3 1 3 3 3 3 3 3 3 3 2 2 3   
## 385 386 387 388 389 390 391 392 393 394 395 396 397 398 399 400   
## 3 3 3 2 3 2 2 3 3 3 2 2 3 3 2 3   
## 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416   
## 3 2 3 2 3 2 3 3 3 3 2 2 3 3 2 2   
## 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 432   
## 3 2 3 3 3 2 2 2 2 2 2 2 3 2 2 3   
## 433 434 435 436 437 438 439 440 441 442 443 444 445 446 447 448   
## 2 1 3 3 3 3 2 3 3 3 3 2 2 3 3 2   
## 449 450 451 452 453 454 455 456 457 458 459 460 461 462 463 464   
## 2 3 2 3 3 3 3 2 3 2 3 2 2 2 2 3   
## 465 466 467 468 469 470 471 472 473 474 475 476 477 478 479 480   
## 2 2 2 3 2 2 2 2 3 3 3 2 3 3 3 3   
## 481 482 483 484 485 486 487 488 489 490 491 492 493 494 495 496   
## 2 3 2 2 2 3 3 3 3 2 3 3 2 3 3 3   
## 497 498 499 500 501 502 503 504 505 506 507 508 509 510 511 512   
## 2 3 3 2 2 2 3 3 2 2 1 3 3 3 3 3   
## 513 514 515 516 517 518 519 520 521 522 523 524 525 526 527 528   
## 3 3 3 3 2 3 3 3 3 3 3 3 3 3 3 3   
## 529 530 531 532 533 534 535 536 537 538 539 540 541 542 543 544   
## 3 3 3 2 2 2 2 2 2 2 3 2 2 2 3 2   
## 545 546 547 548 549 550 551 552 553 554 555 556 557 558 559 560   
## 2 3 2 3 3 2 2 3 3 2 3 3 2 3 2 3   
## 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576   
## 2 3 2 3 2 2 3 2 3 2 2 3 2 3 3 3   
## 577 578 579 580 581 582 583 584 585 586 587 588 589 590 591 592   
## 3 3 3 3 2 3 2 2 3 2 2 3 3 3 2 3   
## 593 594 595 596 597 598 599 600 601 602 603 604 605 606 607 608   
## 2 3 3 3 2 3 3 3 2 3 3 3 3 3 2 2   
## 609 610 611 612 613 614 615 616 617 618 619 620 621 622 623 624   
## 2 1 3 3 2 2 2 2 3 3 3 3 2 2 3 3   
## 625 626 627 628 629 630 631 632 633 634 635 636 637 638 639 640   
## 3 3 2 2 2 3 2 2 3 2 3 3 3 2 2 2   
## 641 642 643 644 645 646 647 648 649 650 651 652 653 654 655 656   
## 3 2 2 2 2 2 3 2 2 2 2 2 2 2 3 3   
## 657 658 659 660 661 662 663 664 665 666 667 668 669 670 671 672   
## 3 3 3 2 3 3 2 3 2 3 3 2 3 2 2 3   
## 673 674 675 676 677 678 679 680 681 682 683 684 685 686 687 688   
## 3 3 2 2 2 3 3 3 3 3 2 2 3 2 3 1   
## 689 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704   
## 2 3 3 2 2 2 2 2 3 2 2 2 2 3 3 3   
## 705 706 707 708 709 710 711 712 713 714 715 716 717 718 719 720   
## 3 3 2 3 2 3 2 3 3 2 3 3 2 2 3 3   
## 721 722 723 724 725 726 727 728 729 730 731 732 733 734 735 736   
## 2 3 3 3 3 3 3 2 3 1 2 2 3 2 2 3   
## 737 738 739 740 741 742 743 744 745 746 747 748 749 750 751 752   
## 2 2 3 3 3 3 3 2 2 3 2 3 2 3 3 2   
## 753 754 755 756 757 758 759 760 761 762 763 764 765 766 767 768   
## 2 2 3 3 2 2 3 3 2 2 2 2 2 3 2 3   
## 769 770 771 772 773 774 775 776 777 778 779 780 781 782 783 784   
## 2 2 3 3 2 2 3 3 3 2 2 2 3 2 2 2   
## 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 800   
## 2 2 2 2 3 2 2 3 2 3 2 2 2 2 3 3   
## 801 802 803 804 805 806 807 808 809 810 811 812 813 814 815 816   
## 2 2 2 2 3 2 2 2 2 2 2 3 3 2 2 3   
## 817 818 819 820 821 822 823 824 825 826 827 828 829 830 831 832   
## 3 2 3 2 3 2 2 3 3 2 2 3 3 3 1 3   
## 833 834 835 836 837 838 839 840 841 842 843 844 845 846 847 848   
## 3 3 1 3 3 3 3 3 3 2 2 3 3 3 2 3   
## 849 850 851 852 853 854 855 856 857 858 859 860 861 862 863 864   
## 2 3 3 2 3 2 3 3 2 2 2 2 3 2 3 3   
## 865 866 867 868 869 870 871 872 873 874 875 876 877 878 879 880   
## 3 3 3 2 2 3 2 2 3 3 3 3 3 3 3 3   
## 881 882 883 884 885 886 887 888 889 890 891 892 893 894 895 896   
## 3 3 3 3 2 3 3 3 3 3 3 3 3 3 3 3   
## 897 898 899 900 901 902 903 904 905 906 907 908 909 910 911 912   
## 2 3 3 2 3 2 2 2 3 3 1 3 2 2 3 3   
## 913 914 915 916 917 918 919 920 921 922 923 924 925 926 927 928   
## 3 3 1 3 3 3 3 3 2 2 2 2 3 3 3 3   
## 929 930 931 932 933 934 935 936 937 938 939 940 941 942 943 944   
## 2 2 3 2 2 2 2 2 3 2 2 2 2 2 3 3   
## 945 946 947 948 949 950 951 952 953 954 955 956 957 958 959 960   
## 2 3 2 3 1 3 3 2 3 3 2 3 3 3 3 2   
## 961 962 963 964 965 966 967 968 969 970 971 972 973 974 975 976   
## 2 3 2 3 2 3 3 2 3 3 3 3 2 3 3 2   
## 977 978 979 980 981 982 983 984 985 986 987 988 989 990 991 992   
## 3 2 3 3 3 3 3 3 3 3 2 2 3 3 3 1   
## 993 994 995 996 997 998 999 1000 1001 1002 1003 1004 1005 1006 1007 1008   
## 2 3 3 3 3 2 2 3 3 2 2 3 3 3 3 3   
## 1009 1010 1011 1012 1013 1014 1015 1016 1017 1018 1019 1020 1021 1022 1023 1024   
## 3 3 3 3 3 2 2 3 2 3 3 2 3 3 3 2   
## 1025 1026 1027 1028 1029 1030 1031 1032 1033 1034 1035 1036 1037 1038 1039 1040   
## 3 3 3 1 3 2 3 2 2 2 2 3 1 1 3 3   
## 1041 1042 1043 1044 1045 1046 1047 1048 1049 1050 1051 1052 1053 1054 1055 1056   
## 1 3 1 2 3 3 3 3 3 3 2 2 3 1 3 3   
## 1057 1058 1059 1060 1061 1062 1063 1064 1065 1066 1067 1068 1069 1070 1071 1072   
## 3 2 3 2 3 2 2 2 3 2 2 3 3 3 3 2   
## 1073 1074 1075 1076 1077 1078 1079 1080 1081 1082 1083 1084 1085 1086 1087 1088   
## 3 2 2 3 2 3 2 2 3 2 2 2 3 2 3 3   
## 1089 1090 1091 1092 1093 1094 1095 1096 1097 1098 1099 1100 1101 1102 1103 1104   
## 2 3 2 2 3 3 2 3 2 3 2 3 2 3 3 3   
## 1105 1106 1107 1108 1109 1110 1111 1112 1113 1114 1115 1116 1117 1118 1119 1120   
## 2 3 3 3 3 2 3 3 2 3 1 3 3 2 3 2   
## 1121 1122 1123 1124 1125 1126 1127 1128 1129 1130 1131 1132 1133 1134 1135 1136   
## 2 3 3 3 3 2 3 3 3 3 3 3 2 3 3 2   
## 1137 1138 1139 1140 1141 1142 1143 1144 1145 1146 1147 1148 1149 1150 1151 1152   
## 3 3 2 3 3 2 2 3 3 2 3 3 3 2 2 2   
## 1153 1154 1155 1156 1157 1158 1159 1160 1161 1162 1163 1164 1165 1166 1167 1168   
## 1 3 2 3 2 2 2 2 3 2 3 2 3 3 3 3   
## 1169 1170 1171 1172 1173 1174 1175 1176 1177 1178 1179 1180 1181 1182 1183 1184   
## 3 3 3 2 3 3 2 2 2 3 2 2 2 2 3 3   
## 1185 1186 1187 1188 1189 1190 1191 1192 1193 1194 1195 1196 1197 1198 1199 1200   
## 3 2 3 3 3 3 3 3 2 2 2 2 3 2 2 3   
## 1201 1202 1203 1204 1205 1206 1207 1208 1209 1210 1211 1212 1213 1214 1215 1216   
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## 3 1 3 3 3 3 3 2 3 3 3 3 3 3 2 3   
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## 3 3 3 3 3 3 3 2 2 3 3 3 3 2 3 3   
## 1249 1250 1251 1252 1253 1254 1255 1256 1257 1258 1259 1260 1261 1262 1263 1264   
## 3 2 3 3 3 3 2 3 3 2 2 2 2 3 3 2   
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## 3 3 3 3 3 3 3 3 3 2 2 3 2 2 3 3   
## 1361 1362 1363 1364 1365 1366 1367 1368 1369 1370 1371 1372 1373 1374 1375 1376   
## 3 3 3 3 3 3 3 2 2 2 3 3 2 2 3 3   
## 1377 1378 1379 1380 1381 1382 1383 1384 1385 1386 1387 1388 1389 1390 1391 1392   
## 3 3 3 3 3 3 3 3 3 1 3 3 3 2 3 3   
## 1393 1394 1395 1396 1397 1398 1399 1400 1401 1402 1403 1404 1405 1406 1407 1408   
## 3 3 3 3 3 2 2 3 2 2 3 3 3 3 3 3   
## 1409 1410 1411 1412 1413 1414 1415 1416 1417 1418 1419 1420 1421 1422 1423 1424   
## 2 3 3 3 3 3 3 3 3 2 3 3 2 3 3 2   
## 1425 1426 1427 1428 1429 1430 1431 1432 1433 1434 1435 1436 1437 1438 1439 1440   
## 3 3 3 3 3 3 3 3 3 3 3 2 2 3 2 2   
## 1441 1442 1443 1444 1445 1446 1447 1448 1449 1450 1451 1452 1453 1454 1455 1456   
## 2 3 3 3 2 3 3 3 3 3 2 3 2 2 2 2   
## 1457 1458 1459 1460 1461 1462 1463 1464 1465 1466 1467 1468 1469 1470 1471 1472   
## 3 3 3 3 3 3 3 3 3 3 3 3 3 3 2 2   
## 1473 1474 1475 1476 1477 1478 1479 1480 1481 1482 1483 1484 1485 1486 1487 1488   
## 3 3 3 3 2 3 3 3 3 3 3 3 2 3 3 2   
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## 2 2 3 3 2 3 3 3 1 3 3 3 3 3 3 3   
## 1505 1506 1507 1508 1509 1510 1511 1512 1513 1514 1515 1516 1517 1518 1519 1520   
## 3 3 2 2 2 3 3 3 3 2 3 3 2 2 3 3   
## 1521 1522 1523 1524 1525 1526 1527 1528 1529 1530 1531 1532 1533 1534 1535 1536   
## 3 3 3 2 2 2 3 2 3 2 2 3 2 3 2 3   
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## 3 3 3 3 2 3 3 3 3 3 2 2 3 3 2 2   
## 1553 1554 1555 1556 1557 1558 1559 1560 1561 1562 1563 1564 1565 1566 1567 1568   
## 3 3 2 3 2 2 2 3 3 1 3 3 1 3 2 3   
## 1569 1570 1571 1572 1573 1574 1575 1576 1577 1578 1579 1580 1581 1582 1583 1584   
## 2 2 2 2 2 3 2 2 3 1 2 2 2 3 3 2   
## 1585 1586 1587 1588 1589 1590 1591 1592 1593 1594 1595 1596 1597 1598 1599 1600   
## 2 2 2 2 2 3 3 2 3 3 2 2 3 2 3 3   
## 1601 1602 1603 1604 1605 1606 1607 1608 1609 1610 1611 1612 1613 1614 1615 1616   
## 2 2 3 3 3 3 3 3 2 2 3 3 3 3 2 3   
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## 2 3 2 3 3 2 2 3 3 2 2 2 3 2 3 3   
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## 3 3 2 3 2 3 2 3 2 2 2 2 2 2 2 3   
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## 3 2 3 2 3 2 2 3 3 2 2 2 2 2 3 2   
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## 2 2 2 2 2 2 2 2 2 3 1 2 3 2 2 3   
## 1697 1698 1699 1700 1701 1702 1703 1704 1705 1706 1707 1708 1709 1710 1711 1712   
## 2 3 3 3 3 2 2 2 2 3 3 2 1 2 3 3   
## 1713 1714 1715 1716 1717 1718 1719 1720 1721 1722 1723 1724 1725 1726 1727 1728   
## 3 3 2 3 3 3 2 3 3 3 2 3 3 2 3 2   
## 1729 1730 1731 1732 1733 1734 1735 1736 1737 1738 1739 1740 1741 1742 1743 1744   
## 2 3 3 2 3 3 2 3 3 2 3 3 2 3 2 2   
## 1745 1746 1747 1748 1749 1750 1751 1752 1753 1754 1755 1756 1757 1758 1759 1760   
## 2 2 3 2 3 3 2 3 2 3 3 2 2 2 3 2   
## 1761 1762 1763 1764 1765 1766 1767 1768 1769 1770 1771 1772 1773 1774 1775 1776   
## 2 3 3 2 2 2 2 2 3 3 2 3 2 2 3 2   
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## 6449 6450 6451 6452 6453 6454 6455 6456 6457 6458 6459 6460 6461 6462 6463 6464   
## 1 1 1 1 1 1 1 1 1 1 1 1 1 1 3 1   
## 6465 6466 6467 6468 6469 6470 6471 6472 6473 6474 6475 6476 6477 6478 6479 6480   
## 1 1 1 1 1 1 2 1 1 1 1 1 1 1 1 1   
## 6481 6482 6483 6484 6485 6486 6487 6488 6489 6490 6491 6492 6493 6494 6495   
## 3 1 1 1 1 1 1 1 1 1 1 1 1 1 3   
##   
## $centers  
## fixed.acidity volatile.acidity citric.acid residual.sugar chlorides  
## 1 0.8629880 1.1712725 -0.319743565 -0.6053435 0.92531224  
## 2 -0.1875822 -0.3411658 0.250318887 1.1324621 -0.09431481  
## 3 -0.3536272 -0.4212641 0.008443436 -0.4304540 -0.45157616  
## free.sulfur.dioxide total.sulfur.dioxide density pH sulphates  
## 1 -0.83706461 -1.18587941 0.6946539 0.53142041 0.8217682  
## 2 0.80789200 0.94373127 0.7238930 -0.38051698 -0.2657525  
## 3 -0.08132816 0.02091816 -0.8777405 -0.03811122 -0.2776704  
## alcohol quality  
## 1 -0.1390639 -0.2913321  
## 2 -0.8028205 -0.3046670  
## 3 0.6217140 0.3688440  
##   
## $totss  
## [1] 77928  
##   
## $withinss  
## [1] 18768.10 13780.69 18963.46  
##   
## $tot.withinss  
## [1] 51512.25  
##   
## $betweenss  
## [1] 26415.75

##calculatING distance of the vectors with the methods of the “euclidean” and “manhattan”, for the linkage OF  
#the HAC “complete” and “average”. #combination of euclidean and complete USED HERE

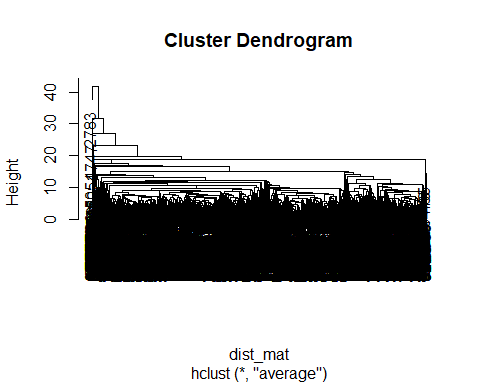
# Calculate distances  
dist\_mat <- dist(predictors, method = 'euclidean')  
#linkage function  
hfitec <- hclust(dist\_mat, method = 'complete')  
plot(hfitec)



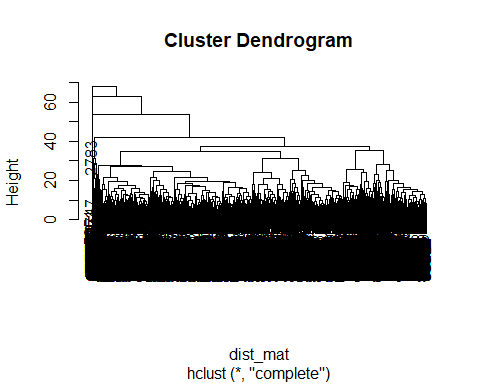
# Calculate distances  
dist\_mat <- dist(predictors, method = 'euclidean')  
#linkage function.  
hfitea <- hclust(dist\_mat, method = 'average')  
plot(hfitea)



#combination of manhattan and average  
# Calculate distances  
dist\_mat <- dist(predictors, method = 'manhattan')  
#linkage function.  
hfitma <- hclust(dist\_mat, method = 'average')  
plot(hfitma)

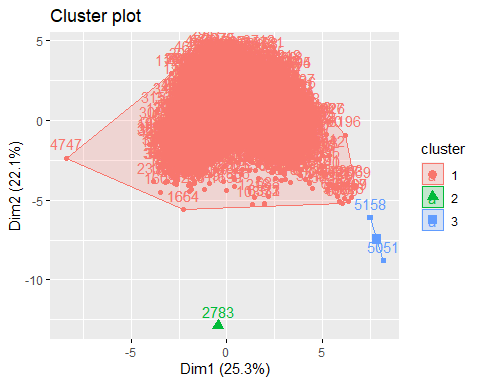


#combination of manhattan and complete  
# Calculate distances  
dist\_mat <- dist(predictors, method = 'manhattan')  
#linkage function.  
hfitmc <- hclust(dist\_mat, method = 'complete')  
plot(hfitmc)

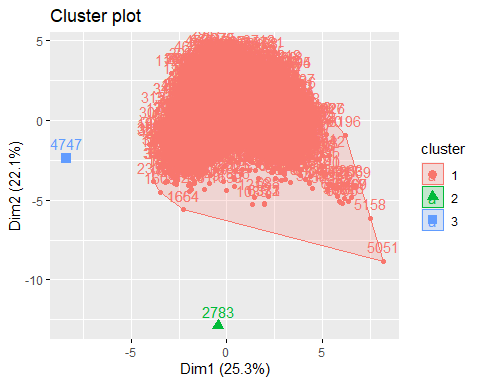


1. Use hierarchical agglomerative clustering (HAC) to cluster the data. Try at least 2 distance functions and at least 2 linkage functions (cluster distance functions), for a total of 4 parameter combinations. For each parameter combination, perform the clustering.

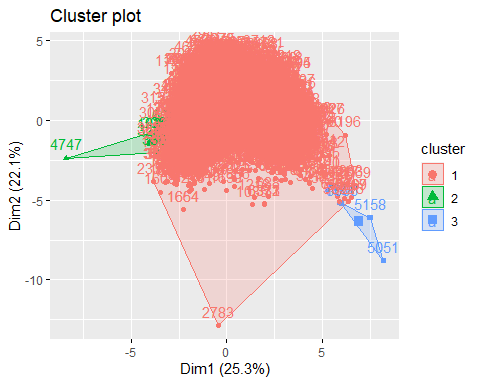
#euclidean and complete  
h1 <- cutree(hfitec, k=3)  
fviz\_cluster(list(data = predictors, cluster = h1))



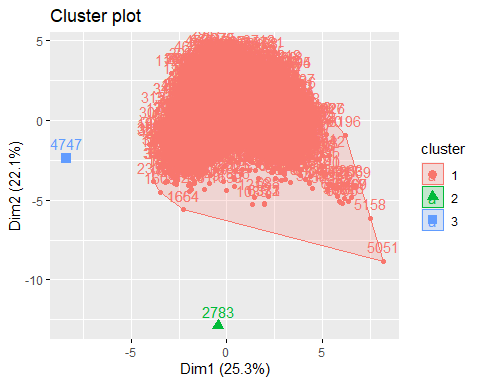
#euclidean and average  
h2 <- cutree(hfitea, k=3)  
fviz\_cluster(list(data = predictors, cluster = h2))



#manhattan and complete  
h4 <- cutree(hfitmc, k=3)  
fviz\_cluster(list(data = predictors, cluster = h4))



#manhattan and average  
h3 <- cutree(hfitma, k=3)  
fviz\_cluster(list(data = predictors, cluster = h3))



1. Compare the k-means and HAC clusterings by creating a crosstabulation between their labels.

#Creating the HAC clustering crosstabulation for H1 which is eculidean and complete  
fit <- kmeans(w\_plot\_d, centers = 4, nstart = 25)  
tab\_ec <- data.frame(Type = wine\_data\_re$type, HAC\_ec = h1, Kmeans = fit$cluster)  
tab\_ec %>% group\_by(HAC\_ec) %>% select(HAC\_ec, Type) %>% table()

## Type  
## HAC\_ec red white  
## 1 1597 4895  
## 2 0 1  
## 3 2 0

#Creating the HAC clustering crosstabulation for H1 which is eculidean and average  
tab\_ea <- data.frame(Type = wine\_data\_re$type, HAC\_ea = h2, Kmeans= fit$cluster)  
tab\_ea %>% group\_by(HAC\_ea) %>% select(HAC\_ea, Type) %>% table()

## Type  
## HAC\_ea red white  
## 1 1599 4894  
## 2 0 1  
## 3 0 1

#Creating the HAC clustering crosstabulation for H1 which is manhattan and complete  
tab\_mc <- data.frame(Type = wine\_data\_re$type, HAC\_mc = h4, Kmeans = fit$cluster)  
tab\_mc %>% group\_by(HAC\_mc) %>% select(HAC\_mc, Type) %>% table()

## Type  
## HAC\_mc red white  
## 1 1595 4888  
## 2 0 8  
## 3 4 0

#Creating the HAC clustering crosstabulation for H1 which is manhattan and average  
tab\_ma <- data.frame(Type = wine\_data\_re$type, HAC\_ma = h3, Kmeans = fit$cluster)  
tab\_ma %>% group\_by(HAC\_ma) %>% select(HAC\_ma, Type) %>% table()

## Type  
## HAC\_ma red white  
## 1 1599 4894  
## 2 0 1  
## 3 0 1

#Creating the Kmeans crosstabulation for eculidean and complete  
tab\_ec %>% group\_by(Kmeans) %>% select(Kmeans, Type) %>% table()

## Type  
## Kmeans red white  
## 1 55 1935  
## 2 2 1099  
## 3 305 1727  
## 4 1237 135

#Creating the Kmeans crosstabulation for eculidean and average  
tab\_ea %>% group\_by(Kmeans) %>% select(Kmeans,Type) %>% table()

## Type  
## Kmeans red white  
## 1 55 1935  
## 2 2 1099  
## 3 305 1727  
## 4 1237 135

#Creating the Kmeans crosstabulation for manhattan and complete  
tab\_mc %>% group\_by(Kmeans) %>% select(Kmeans, Type) %>% table()

## Type  
## Kmeans red white  
## 1 55 1935  
## 2 2 1099  
## 3 305 1727  
## 4 1237 135

#Creating the Kmeans crosstabulation for manhattan and average  
tab\_ma %>% group\_by(Kmeans) %>% select(Kmeans, Type) %>% table()

## Type  
## Kmeans red white  
## 1 55 1935  
## 2 2 1099  
## 3 305 1727  
## 4 1237 135

1. For comparison – use PCA to visualize the data in a scatterplot. Create 3 separate plots: use the color of the points to show (1) the type label, (2) the k-means cluster labels and (3) the HAC cluster labels.

rwine3 <- rwine  
wwine3 <- wwine  
wwine3$type <- "white"  
rwine3$type <- "red"  
wine\_data <- full\_join(wwine3,rwine3)

## Joining, by = c("fixed.acidity", "volatile.acidity", "citric.acid",  
## "residual.sugar", "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide",  
## "density", "pH", "sulphates", "alcohol", "quality", "type")

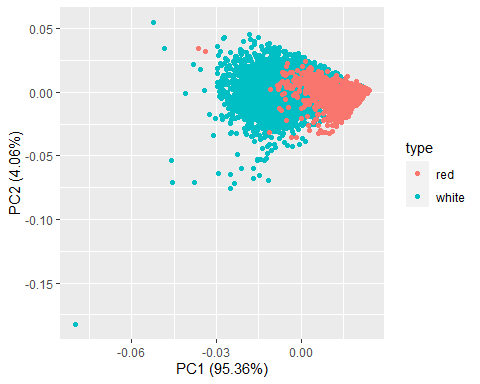
wine\_data <- na.omit(wine\_data)  
str(wine\_data)

## 'data.frame': 6497 obs. of 13 variables:  
## $ fixed.acidity : num 7 6.3 8.1 7.2 7.2 8.1 6.2 7 6.3 8.1 ...  
## $ volatile.acidity : num 0.27 0.3 0.28 0.23 0.23 0.28 0.32 0.27 0.3 0.22 ...  
## $ citric.acid : num 0.36 0.34 0.4 0.32 0.32 0.4 0.16 0.36 0.34 0.43 ...  
## $ residual.sugar : num 20.7 1.6 6.9 8.5 8.5 6.9 7 20.7 1.6 1.5 ...  
## $ chlorides : num 0.045 0.049 0.05 0.058 0.058 0.05 0.045 0.045 0.049 0.044 ...  
## $ free.sulfur.dioxide : num 45 14 30 47 47 30 30 45 14 28 ...  
## $ total.sulfur.dioxide: num 170 132 97 186 186 97 136 170 132 129 ...  
## $ density : num 1.001 0.994 0.995 0.996 0.996 ...  
## $ pH : num 3 3.3 3.26 3.19 3.19 3.26 3.18 3 3.3 3.22 ...  
## $ sulphates : num 0.45 0.49 0.44 0.4 0.4 0.44 0.47 0.45 0.49 0.45 ...  
## $ alcohol : num 8.8 9.5 10.1 9.9 9.9 10.1 9.6 8.8 9.5 11 ...  
## $ quality : int 6 6 6 6 6 6 6 6 6 6 ...  
## $ type : chr "white" "white" "white" "white" ...

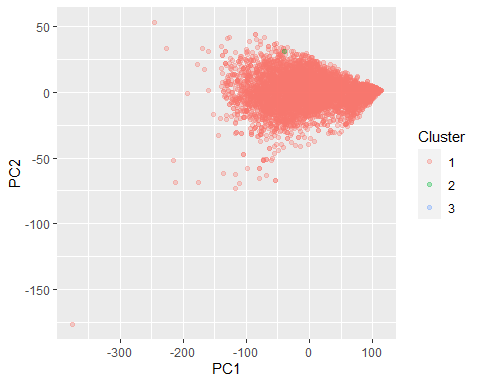
wine\_data\_re <- wine\_data[-c(56,78),]  
str(wine\_data\_re)

## 'data.frame': 6495 obs. of 13 variables:  
## $ fixed.acidity : num 7 6.3 8.1 7.2 7.2 8.1 6.2 7 6.3 8.1 ...  
## $ volatile.acidity : num 0.27 0.3 0.28 0.23 0.23 0.28 0.32 0.27 0.3 0.22 ...  
## $ citric.acid : num 0.36 0.34 0.4 0.32 0.32 0.4 0.16 0.36 0.34 0.43 ...  
## $ residual.sugar : num 20.7 1.6 6.9 8.5 8.5 6.9 7 20.7 1.6 1.5 ...  
## $ chlorides : num 0.045 0.049 0.05 0.058 0.058 0.05 0.045 0.045 0.049 0.044 ...  
## $ free.sulfur.dioxide : num 45 14 30 47 47 30 30 45 14 28 ...  
## $ total.sulfur.dioxide: num 170 132 97 186 186 97 136 170 132 129 ...  
## $ density : num 1.001 0.994 0.995 0.996 0.996 ...  
## $ pH : num 3 3.3 3.26 3.19 3.19 3.26 3.18 3 3.3 3.22 ...  
## $ sulphates : num 0.45 0.49 0.44 0.4 0.4 0.44 0.47 0.45 0.49 0.45 ...  
## $ alcohol : num 8.8 9.5 10.1 9.9 9.9 10.1 9.6 8.8 9.5 11 ...  
## $ quality : int 6 6 6 6 6 6 6 6 6 6 ...  
## $ type : chr "white" "white" "white" "white" ...

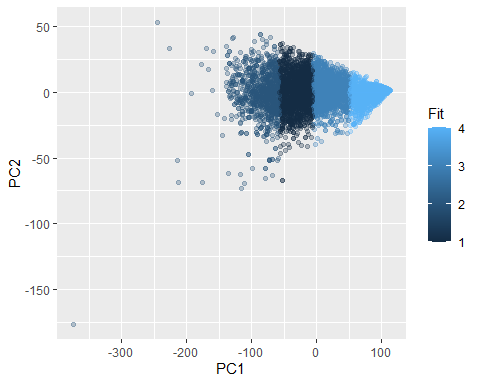
#plot for type of label  
#PCA scaling for the raw data  
wine\_data\_pcascaling <- prcomp(wine\_data\_re[, c(1:11,12)])  
library(ggfortify)  
autoplot(wine\_data\_pcascaling, data = wine\_data\_re, colour = "type")



#Clustering w rotated dataset.  
pca <- prcomp(w\_plot\_d)# Calculate PCA  
rotated\_data = as.data.frame(pca$x)  
rotated\_data$Cluster <- as.factor(h1)  
ggplot(data = rotated\_data, aes(x = PC1, y = PC2, col = Cluster)) + geom\_point(alpha = 0.3)



#plot for Kmeans w rotated dataset.  
rotated\_data$Fit <- fit$cluster  
ggplot(data = rotated\_data, aes(x = PC1, y = PC2, col = Fit)) + geom\_point(alpha = 0.3)



1. Consider the results of C and D and explain the differences between the clustering results in terms of how the algorithms work.

##Inference:  
#The K-means is dependendent on the K value for clustering on the other hand the HAC cluster are purely based on the  
#similarities bwtween the vectors. To add on, K-means have the centroid value.The processing speed factor is better for Kmeans than HAC. K-means compute with distance whereas HAC compute to the last vector of the given data table.